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Many roads to symmetry breaking: molecular mechanisms and theoretical models of yeast cell polarity

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ABSTRACT Mathematical modeling has been instrumental in identifying common principles of cell polarity across diverse systems. These principles include positive feedback loops that are required to destabilize a spatially uniform state of the cell. The conserved small G-protein Cdc42 is a master regulator of eukaryotic cellular polarization. Here we discuss recent developments in studies of Cdc42 polarization in budding and fission yeasts and demonstrate that models describing symmetry-breaking polarization can be classified into six minimal classes based on the structure of positive feedback loops that activate and localize Cdc42. Owing to their generic system-independent nature, these model classes are also likely to be relevant for the G-protein-based symmetry-breaking systems of higher eukaryotes. We review experimental evidence pro et contra different theoretically plausible models and conclude that several parallel and non-mutually exclusive mechanisms are likely involved in cellular polarization of yeasts. This potential redundancy needs to be taken into consideration when interpreting the results of recent cell-rewiring studies.

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INTRODUCTION

Eukaryotic cell polarization is a fundamental process that involves formation of a persistent morphological axis akin to a compass needle (Bourne and Weiner, 2002). The transition from an unpolarized state with all spatial directions potentially equal to a state with one specific direction chosen, or *symmetry breaking*, continues to puzzle and fascinate researchers across many disciplines. The intellectual appeal of cell polarization, as well as its biological importance, has driven significant experimental and theoretical effort in understanding the basic mechanisms of cell polarity. This work established the existence of evolutionarily conserved polarity proteins and common biophysical principles but also revealed staggering diversity, redundancy, and

mutability of polarity mechanisms (Drubin and Nelson, 1996; Martin-Belmonte and Mostov, 2008; McCaffrey and Macara, 2012).

Here we focus on the molecular mechanisms and theoretical models of cell polarity establishment in budding and fission yeasts. Based on decades of genetic studies, we now have an almost complete list of “players”—yeast proteins involved in the polarity mechanisms (Drees et al., 2001). Although we do not yet fully understand how these players act together, in yeasts, we are perhaps the closest to the dream of mechanistic modeling—to be able to match any model variable to a specific protein and every arrow to a particular biochemical reaction. In addition to classical genetic methods, “cell-rewiring” approaches have become increasingly popular. These studies deployed synthetic proteins to purposefully change the layout of molecular networks, for example, by altering cellular localization of specific players. These efforts, frequently initiated to test the validity of preexisting conceptual models, generated alternative models of their own. The resulting proliferation of the rewired mutants, new mathematical models, and unfamiliar jargon borrowed from physical and mathematical sciences make it difficult to follow progress in the field. Here we review these recent developments and show that the existing models fall within a few well-delimited conceptual classes. Surprisingly, we conclude that, beyond the already proposed models, additional model classes are theoretically possible and, at least in part, are supported by experimental data. We argue that, simple as they may

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Abbreviations used: FRAP, fluorescence recovery after photobleaching; GAP, GTPase-activating protein; GDP, guanosine diphosphate; GEF, guanine-nucleotide exchange factor; GTP, guanosine triphosphate; MAPK, mitogen-activated protein kinase.

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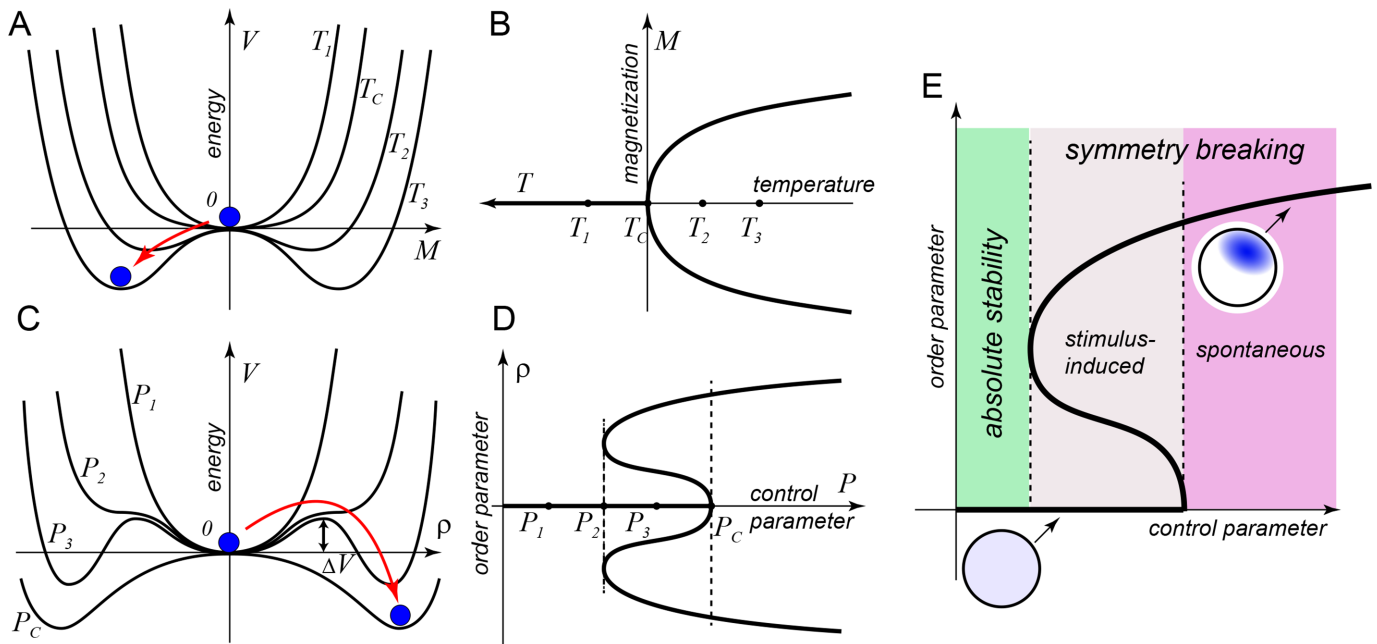


FIGURE 1: Symmetry breaking in physics and biology. (A, B) Transition of paramagnetic to ferromagnetic state as a prototypical example of symmetry breaking. (A) Symmetric state $M = 0$ changes from the energy minimum to a local maximum at the Curie temperature. (B) At the transition point, the system selects one of two equivalent branches. (C, D) A system in which the symmetric state $\rho = 0$ remains locally stable after asymmetric states are born. (C) The system can be forced out of the symmetric state if the energy barrier is exceeded. (D) Multistable parameter region corresponds to an energy function with three minima. (E) Symmetry breaking in a biological system far from thermodynamic equilibrium. Nonzero order parameter corresponds to the emergence of spatial structure. Spatially homogeneous and polarized states of the system are shown schematically as uniform and patterned spherical cells, respectively.

appear in comparison with higher eukaryotes, yeasts likely possess multiple redundant mechanisms of symmetry breaking. This conclusion calls for a caution in interpreting the results of recent studies directed at identifying “the correct” model of yeast cell polarity.

SYMMETRY BREAKING: FROM PHYSICS TO BIOLOGY

The notion of spontaneous symmetry breaking (Baker and Glashow, 1962) originated in particle physics, rapidly spread across all of physics, and gained prominence as one of its central unifying concepts (Bijker, 2009). A classical example of spontaneous symmetry breaking is the ferromagnetic phase transition that occurs at the Curie temperature, T_c (Figure 1, A and B). When temperature (the control parameter) is above critical, $T > T_c$, the matter is in the paramagnetic phase, which is symmetric, in the sense that all directions of atomic magnetic dipoles are equally probable, and the average value of magnetization, M (the order parameter), is 0. For $T \leq T_c$, the paramagnetic state, $M = 0$, is no longer the minimum of potential energy but, instead, its local maximum. This means that the symmetric state, $M = 0$, becomes absolutely unstable, and the system randomly selects a new energy minimum out of infinitely many equienergetic ferromagnetic states with a nonzero average magnetization and, therefore, broken rotational symmetry.

Consider now a different example of symmetry breaking with a more complex shape of energy function, $V(\rho)$ (Figure 1, C and D). Here there is a range of control parameter values, $P_2 < P < P_c$, within which energy has three minima. If the control parameter is increased from, say, P_1 to P_3 , the system that at P_1 was in the symmetric state, $\rho = 0$, will remain there at P_3 , even though the asymmetric states have lower energy. The state of the system will remain unchanged until a sufficiently large perturbation throws it over the energy barrier, ΔV , that separates the states. If the control parameter

continues to increase, the symmetric state, $\rho = 0$, becomes absolutely unstable at $P = P_c$, just as in the ferromagnetic example. However, in the second example, before this spontaneous transition, the system can be forced to undergo symmetry breaking. This requires an external stimulus with amplitude larger than a certain threshold.

Prigogine and colleagues proposed that the Turing mechanism for the spontaneous emergence of spatial organization via the diffusion-driven instability of a spatially homogeneous state (Turing, 1952), or *Turing instability*, can be considered a spontaneous symmetry-breaking transition (Prigogine and Nicolis, 1967; Prigogine et al., 1969). They foresaw that this type of symmetry breaking plays an important role in biology and demonstrated that it can happen only in systems far from thermodynamic equilibrium. Although the useful concept of potential energy is no longer well defined in these systems, they behave surprisingly similarly to equilibrium systems (Figure 1E). Just as in equilibrium phase transitions, there exists a critical parameter value beyond which the spatially homogeneous state is unstable to any perturbation, including thermal molecular noise. Between the domains of absolute stability and instability of the “symmetric” state lies an area where symmetry can be broken by a superthreshold stimulus.

By now the concept of symmetry breaking has firmly established itself in biology (Kirschner et al., 2000; Atkins et al., 2008; Li and Bowerman, 2010). Whereas the original idea of Turing was based on the interplay of chemical reactions and diffusion, the “multiphysics” nature of biological systems calls for a much broader exploration for causes of symmetry breaking. Indeed, hydrodynamic (Gowrishankar et al., 2012; Tjhung et al., 2012), mechanical (Howard et al., 2011; Maiuri et al., 2015), and electrical (Hombel and Leonetti, 2007; Chang and Minc, 2014) forces can also drive symmetry breaking when coupled with nonlinear chemical reactions, with each other, or even on their own.

Physiologically, symmetry breaking in biological systems is guided by certain “cues,” stimuli that are either intrinsic, also known as “landmarks,” or extrinsic, such as gradients of signaling molecules detected by sensors. Stimulus-induced transitions provide the ability to sense and amplify environmental cues that exceed the level of background noise. Thus it appears that, under normal physiological conditions, biological systems are maintained within the region of parameters corresponding to the bistable state, posed for the stimulus-induced symmetry breaking (Figure 1E). Accordingly, much effort has been put into the characterization of cues that initiate the symmetry-breaking transition. Nonetheless, it was the experimental decoupling of inputs from landmarks and sensors that permitted discovery of the existence of spontaneous cell-intrinsic symmetry-breaking mechanisms in various organisms.

CELL POLARIZATION IN YEAST AND ITS RELATION TO SYMMETRY BREAKING

In the budding yeast *Saccharomyces cerevisiae*, cell polarization has been historically associated with polarized cell growth during vegetative budding and formation of a mating protrusion, also known as a shmoo (Drubin, 1991; Pruyne and Bretscher, 2000; Bi and Park, 2012). The fission yeast *Schizosaccharomyces pombe* also forms polarized mating protrusions, but, instead of budding, it exhibits polarized vegetative growth localized to one or both tips of its cylindrical cell. Polarized growth in yeasts is attributed to the localized insertion of secretory vesicles that stream along the actin cables directed toward the sites of polarized growth. Polarization of actin cytoskeleton, revealed by both the organization of actin cables and localization of endocytic actin patches, together with polarization of membrane insertion and cell wall remodeling have been frequently used as distinctive signs of yeast cell polarity (Drubin, 1991).

Already early genetic analyses identified the small Rho GTPase Cdc42 as an essential regulator of cell polarization (Adams et al., 1990; Johnson and Pringle, 1990). A breakthrough in understanding the role of Cdc42 in yeast polarity was made possible by the introduction of Cdc42 activity reporters (Nalbant et al., 2004; Ozbudak et al., 2005; Tong et al., 2007). These probes are fusions of fluorescent proteins with the Cdc42-binding (or CRIB) domains of Cdc42 effectors, proteins that interact preferentially with the GTP-bound, or active, form of Cdc42 (Burbelo et al., 1995). Live-cell imaging studies with CRIB reporters demonstrated that, in budding yeast, an approximately round cluster of Cdc42-GTP emerges at the presumptive bud site (PBS) well in advance of the beginning of bud protrusion (Ozbudak et al., 2005; Tong et al., 2007; Okada et al., 2013). Formation of this cluster of Cdc42-GTP, as reported by the CRIB activity probe, and local enrichment in total Cdc42, as reported by direct labeling of the GTPase with fluorescent proteins, is frequently referred to as *Cdc42 polarization*. Similar clusters of Cdc42-GTP are routinely observed at the growing tips of fission yeast cells, as well as in germinating spores and at the mating protrusions in both yeasts (Bonazzi et al., 2014; Martin, 2015).

Treatment of budding yeast with latrunculin A (Lat A) depolymerizes both cables and endocytic patches (Ayscough et al., 1997) but does not prevent either emergence or maintenance of clusters of Cdc42-GTP (Ayscough et al., 1997; Irazoqui et al., 2003; Okada et al., 2013). Furthermore, application of Lat A to cells deleted for one or more Cdc42 inactivators, GTPase-activating proteins (GAPs), demonstrated that in these cells, overactive Cdc42-GTP clusters can drive pronounced polarized cell growth in the absence of cables (Okada et al., 2013). However, in fission yeast, Lat A disperses Cdc42-GTP clusters from the cell tips (Bendezu and Martin, 2011; Bendezu et al., 2015). On the surface, this result could have been considered

as supporting the notion that Cdc42 polarization depends on actin cytoskeleton, at least in *S. pombe*. However, it should be kept in mind that, in addition to depolymerizing F-actin, Lat A also induces a cell stress response via the stress-activated mitogen-activated protein kinases (MAPKs; McMillan et al., 1998; Harrison et al., 2004). A recent study in *S. pombe* unequivocally demonstrates that Lat A induces stress-activated MAPK Sty1 and inhibition of Sty1 activation prevents Cdc42 depolarization despite the complete depolymerization of the actin cytoskeleton (Mutavchiev et al., 2016). Thus, in both yeasts, actin cytoskeleton per se is not required for Cdc42 polarization. A more complex subject—the requirement for polarized secretion in Cdc42 polarization—remains a matter of controversy. Regardless of the relationships between various constituents of polarized growth, emergence of the Cdc42-GTP cluster has become the de facto criterion for judging whether a given set of experimental conditions permits or prevents cellular polarization. Therefore in the following we focus on the molecular mechanisms and theoretical models of Cdc42 polarization.

Does symmetry breaking play any role in Cdc42 polarization? In budding yeast, Cdc42 polarization is directed by the budding landmarks and signaling of G-proteins that are activated downstream of mating pheromones (Butty et al., 1998; Park and Bi, 2007; Bi and Park, 2012). Landmarks ensure that, in haploid yeasts, a new bud forms right next to the budding scar from the previous cell cycle (axial pattern), whereas in diploid cells, buds form in the alternating bipolar pattern. Multiple landmark systems engage the Cdc42 polarity module via a single common element, a Ras-like GTPase Rsr1/Bud1 (Bender and Pringle, 1989). In *rsr1Δ* cells, spatially uniform activity of CDK1 increases the control parameter (in this case, the cytoplasmic concentration of the Cdc42 activator) until Cdc42 polarization emerges at a random cortical location, apparently via spontaneous symmetry breaking (Irazoqui et al., 2003). However, even in the presence of landmarks, polarization can satisfy the criteria for symmetry breaking. Indeed, the landmarks are physically positioned in a circle surrounding the birth scar, that is, with circular symmetry, $0 < \phi < 2\pi$, whereas the bud forms at a particular location, $\phi = \phi_0$, just outside of this circle. Thus a random noise-driven choice breaks the circular symmetry of landmark distribution (Wu et al., 2013). Unfortunately, Rsr1 is not conserved in fission yeast, and the exact relationship between the fission yeast landmarks and the Cdc42 module is not well understood. In all fungi, spore germination is possibly the most biologically relevant scenario in which polarization of Cdc42 occurs via symmetry breaking naturally, without experimental intervention (Bonazzi et al., 2014; Lichius et al., 2014; Bendezu et al., 2015).

Mathematical models that attempt to explain spontaneous Cdc42 polarization should be able to describe spontaneous symmetry breaking. This means that within a reasonably broad domain of parameters, their spatially uniform steady state should be unstable to infinitesimally small perturbations, that is, exhibit Turing instability. Landmarks and sensory inputs can be readily added to such models by, for example, spatially dependent initial conditions. A less constrained and therefore much larger set of models can describe amplification of Cdc42 activity or enrichment in response to a spatially dependent template of activation or transport. However, the majority of these models will lose Cdc42 polarization as soon as this input is withdrawn. Thus, for a model that attempts to explain spontaneous Cdc42 polarization in yeast, the ability to sustain polarization in the steady state, long after the initial perturbation that biased the symmetry breaking has vanished, is the necessary condition of applicability. A number of models assumed a preexisting polarization of actin cables (Wedlich-Soldner et al., 2003; Marco et al., 2007; Slaughter et al., 2009, 2013; Das et al., 2012). In these

models, spatial symmetry is broken from the outset by the model design, and the authors instead focus their attention on how the spatial distribution of Cdc42 might follow that of the actin cables. In the following discussion, we restrict our attention to models that can describe spontaneous symmetry breaking.

The processes that enable Cdc42 polarization include translocation to and away from the site of polarization, local cycles of activation/inactivation, and, finally, diffusion on the plasma membrane, all of which depend on interactions with other cellular proteins and membrane lipids (Park and Bi, 2007; Ridley, 2015). The nucleotide state of Cdc42 is controlled by activating nucleotide exchange factors (GEFs), which catalyze the exchange of Cdc42-bound GDP to GTP, and inactivating GAPs, which accelerate the hydrolysis of GTP by Cdc42. The GTP-bound, or active, form of Cdc42 (denoted RT in the formulas and diagrams) has a conformation distinct from that of the GDP-bound form (RD). Proteins capable of detecting this conformation difference, for example, effectors, interact differentially with active and inactive forms. This makes RT and RD effectively distinct chemical species that are interconverted by the cycles of activation/inactivation. In the language of chemical kinetics, the rate of change of the local concentration of Cdc42-GTP can be expressed formally as

$$\frac{d}{dt}RT = \dot{RT} = \text{rate of activation} - \text{rate of inactivation} = F_{\text{act}} - F_{\text{inact}} \quad (1)$$

and the rate of change of RD by an expression in which the signs of the rates of activation and inactivation are reversed. Because both processes are enzymatic reactions, their rates are generally described by the familiar Michaelis–Menten formula. However, if GEFs and GAPs function far from saturation, the rates of activation and inactivation become simply the rates of two bimolecular reactions:

$$\dot{RT} = k_E \cdot [\text{GEF}] \cdot RD - k_A \cdot [\text{GAP}] \cdot RT = E \cdot RD - A \cdot RT. \quad (2)$$

Assuming for now that the system is spatially homogeneous, we find that Eq. 2 has a simple steady-state solution. Because in the steady state $\dot{RT} = 0$, we get $RT/RD = E/A$. This steady state is, in fact, stable. Intuitively, this can be seen directly from Eq. 2. If we try to perturb the steady state by activating Cdc42, that is, converting some RD into RT, the rate of activation will drop while the rate of inactivation will increase, and the system will return back.

HOW MUCH POSITIVE FEEDBACK IS NEEDED FOR SYMMETRY BREAKING?

Because symmetry breaking is associated with instability of the pre-existing steady state, to achieve Cdc42 polarization, it is necessary that the rate of activation grows faster with the increase in RT than the rate of inactivation. Here we also assume that the total cellular amount of the GTPase is conserved during the transition. Then, if $F_{\text{act}} \sim RT^n$ and $F_{\text{inact}} \sim RT^m$, for the symmetry breaking to occur, it is required that $n > m$. This condition can be satisfied only in the presence of feedback, that is, when the local rates of Cdc42 activation, inactivation, or both depend on the activity of Cdc42 itself.

The crucial role of feedback in the emergence of complex behavior, such as bistability, oscillations, and spatial structures, has been well understood mathematically and is by now firmly established in biology (Novak and Tyson, 2008; Ferrell, 2013). In Cdc42 polarization, positive feedback can emerge via a number of nonexclusive scenarios—for example, if Cdc42 activity is involved in the recruitment to the site of polarization of GEFs or Cdc42 itself. A double-negative loop in which Cdc42 activity causes reduction in the activity of a GAP will also generate a cumulative positive

feedback loop. Of interest, theorists noticed that a single positive feedback loop does not provide symmetry breaking in the models of cell polarization (Lo et al., 2014). A notable exception was reported in a stochastic model of budding yeast cell polarity (Altschuler et al., 2008). That a single positive feedback loop is not sufficient to break symmetry, at least within the deterministic approach, can be illustrated using Eqs. 1 and 2. For example, if either a GEF or inactive Cdc42 can be recruited to the site of polarization by the activity of Cdc42, the rate of activation will be proportional to RT, and thus $n = 1$. However, Eq. 2 shows that $F_{\text{inact}} \sim RT$, and therefore $n = m = 1$, and the condition $n > m$ is not satisfied.

Multiple feedback loops are commonly found in biological molecular networks. However, the presence of several feedback loops by itself does not yet guarantee symmetry breaking. In a hypothetical cell in which Cdc42 is activated by two distinct GEFs both recruited to the membrane by the Cdc42 activity, the rate of Cdc42 activation is a sum of two functions, $F_{\text{act}}(\text{GEF1}) + F_{\text{act}}(\text{GEF2})$, each proportional to RT, and the outcome does not differ from that in the case of a single feedback loop. This is a typical example of *parallel* feedback loops. To achieve symmetry breaking, feedback loops must be *converging*, or *cooperating* (Lo et al., 2014). Convergence of feedback loops (Figure 2A) can be exemplified by a hypothetical scenario in which both a GEF and RD are recruited to the membrane by the activity of Cdc42. Because the activation of Cdc42 by its GEF is a bimolecular reaction, according to the mass-action rate law of chemical kinetics, its rate is proportional to the product of the local concentrations of the two molecules:

$$F_{\text{act}} = k_E \cdot [\text{GEF}](RT) \cdot RD(RT) \sim RT^2 \quad (3)$$

This makes $n = 2$, and, if $m = 1$ as in Eq. 2, the condition for symmetry breaking is satisfied.

Positive feedback loops are sufficient to enable symmetry-breaking polarization. Addition of negative feedback dramatically increases the range of spatiotemporal patterns that can be observed in biological systems. In models of yeast polarity, additional negative feedback produces Cdc42-GTP clusters that move, oscillate in place, or jump between different locations on the cell cortex (Ozbudak et al., 2005; Howell et al., 2012; Dyer et al., 2013; Okada et al., 2013; Wu and Lew, 2013; McClure et al., 2015).

SIX MECHANISTIC METAMODELS OF CDC42 POLARIZATION

We can modify Eq. 2 by introducing an arbitrary number of converging positive feedback loops that affect concentrations of GEFs and GAPs and inactive Cdc42:

$$\dot{RT} = E(RT^k) \cdot RD(RT^l) - A(RT^{m-1}) \cdot RT = F_{\text{act}}(RT^{k+l}) - F_{\text{inact}}(RT^m) \quad (4)$$

In Eq. 4, we explicitly distinguish k feedback loops converging on the recruitment of a GEF from l converging feedback loops that control the concentration of inactive Cdc42. The condition for symmetry breaking then becomes

$$k + l > m \quad (5)$$

Inequality 5 can be satisfied by a great many potential models. However, if we request that the models must have minimal complexity, that is, that the total number of all feedback loops is kept to a minimum and $k + l - m = 1$, we find that all minimal models with symmetry breaking fall within six classes. These classes can be mathematically represented by distinct combinations of small integer numbers k , l , and m that satisfy inequality 5.

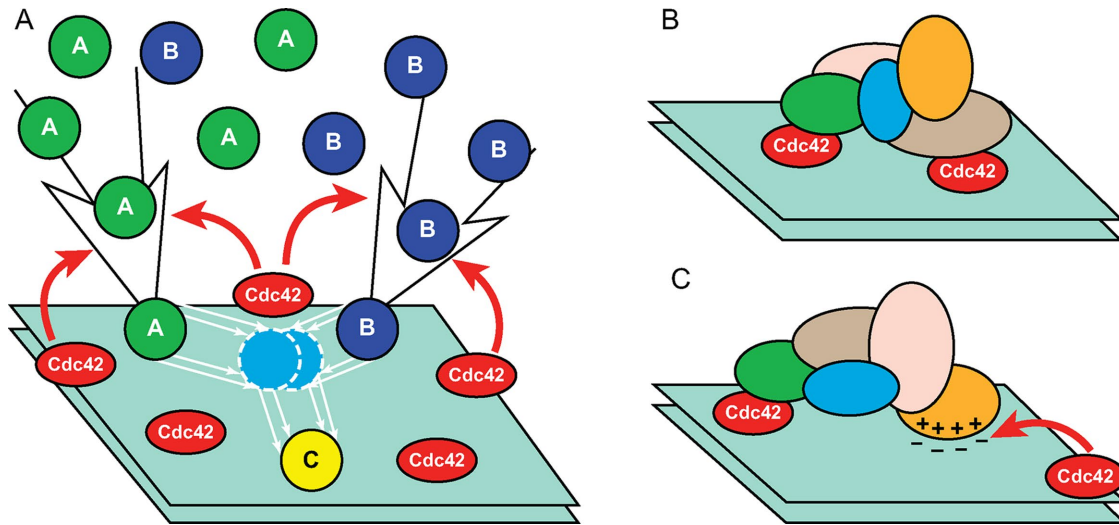


FIGURE 2: Sources of nonlinearity in the Cdc42 polarity module. (A) If reaction $A + B \rightarrow C$ takes place on the membrane and both A and B are recruited downstream of Cdc42 activity, the rate of production of C is proportional to the square of Cdc42-GTP concentration. (B) The membrane concentration of a protein complex that interacts with the membrane via two independent Cdc42 effectors (or one bivalent effector) is proportional to the square of Cdc42-GTP concentration. (C) Similar to B, but in this case, one of the complex subunits interacts with negatively charged phospholipids whose accumulation is downstream of Cdc42 activity.

Model A. Converging linear feedback via GEF and RD ($k = 1, l = 1, m = 1$)

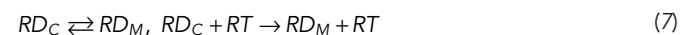
In budding yeast, Cdc42 effector Bem1 forms a stable complex with the only Cdc42 GEF, Cdc24. Recruitment of Cdc24 by Cdc42-GTP via Bem1 constitutes a Cdc42 autoactivation loop that has been shown to be necessary for Cdc42 polarization (Gulli *et al.*, 2000; Bose *et al.*, 2001; Butty *et al.*, 2002; Irazoqui *et al.*, 2003). The feedback complex also includes another Cdc42 effector, Pak kinase Cla4 (Kozubowski *et al.*, 2008). Bem1 is conserved among fungi, and its fission yeast homologue, Scd2, plays a similar role in recruiting GEF Scd1 (Chang *et al.*, 1994). Consequently a number of yeast polarity models, in addition to unaided membrane-cytoplasmic shuttling of GEF, rely on the existence of a positive feedback loop in which a cytosolic GEF is recruited by active Cdc42 via an effector:



where E_C and E_M are the cytoplasmic and membrane-bound GEF-effector complexes, respectively. We consider RT to be membrane bound and omit the subscript M as redundant.

Because a single linear positive feedback loop is insufficient to provide symmetry breaking, the necessary additional feedback loop can come from the recruitment of Cdc42 itself (Figure 3A). Several mutually nonexclusive mechanisms can be proposed here. Yeast Cdc42 in its inactive form can be delivered to the plasma membrane by secretory vesicles (Watson *et al.*, 2014; Bendezu *et al.*, 2015). Secretion in yeasts is positively regulated by Cdc42-GTP via at least two parallel pathways: tethering of vesicles to the plasma membrane and, independently, regulation of actin cable polymerization (Bendezu and Martin, 2011). In the former pathway, the effector in question is the exocyst, a multiprotein complex several subunits of which have been shown to interact with Cdc42-GTP (Adamo *et al.*, 2001; Zhang *et al.*, 2001, 2008; Wu *et al.*, 2010a). In the latter pathway, formins that synthesize the cables (Bni1 and Bnr1 in budding and For3 in fission yeast) are believed

to interact with Cdc42-GTP either directly (Martin *et al.*, 2007) or via other effectors (Chen *et al.*, 2012). Cdc42 can also travel through the cytoplasm diffusively either in a complex with GDP dissociation inhibitors (GDIs) or on its own (Johnson *et al.*, 2009; Zhang *et al.*, 2014). In both budding and fission yeast, Cdc42 attaches to membranes by the C-terminal prenyl (geranylgeranyl) moiety and a short polybasic cluster of four lysine residues (+4). Cdc42-induced local increase in the membrane negative charge due, for example, to the flippase-mediated enrichment of phosphatidylserine (Das *et al.*, 2012; Bruurs *et al.*, 2015) could provide a positive feedback loop that would work for both GDI-dependent (Ugolev *et al.*, 2006, 2008) and GDI-independent routes of Cdc42 diffusive transport. Other lipid-mediated mechanisms of positive feedback are also possible because negatively charged phosphoinositides phosphatidylinositol-4,5-bisphosphate and phosphatidylinositol-4-phosphate have also been shown to be enriched at the sites of cellular polarization (Garrenton *et al.*, 2010; Ghugtyal *et al.*, 2015). An additional potential GDI-dependent feedback mechanism involves the Cdc42 effector kinase Cla4, which was reported to reduce the interaction between budding yeast GDI Rdi1 and Cdc42 and increase deposition of the GTPase on the membrane (Tiedje *et al.*, 2008). Similar to reaction 6, each of the foregoing molecular mechanisms in aggregate can be represented by cumulative expressions:



Together reactions 6 and 7 ensure that the concentrations of both membrane-bound GEF and RD depend on RT and satisfy the symmetry-breaking condition.

Of importance, the two feedback loops in this model class need not be independent. Wedlich-Söldner, Frey, and colleagues proposed a model (Freisinger *et al.*, 2013; Klunder *et al.*, 2013) in which Cdc42-GTP recruits Cdc24 via Bem1, whereas Cdc24, in turn, recruits cytoplasmic Cdc42-GDP (dashed arrow in Figure 3A) and simultaneously activates it:

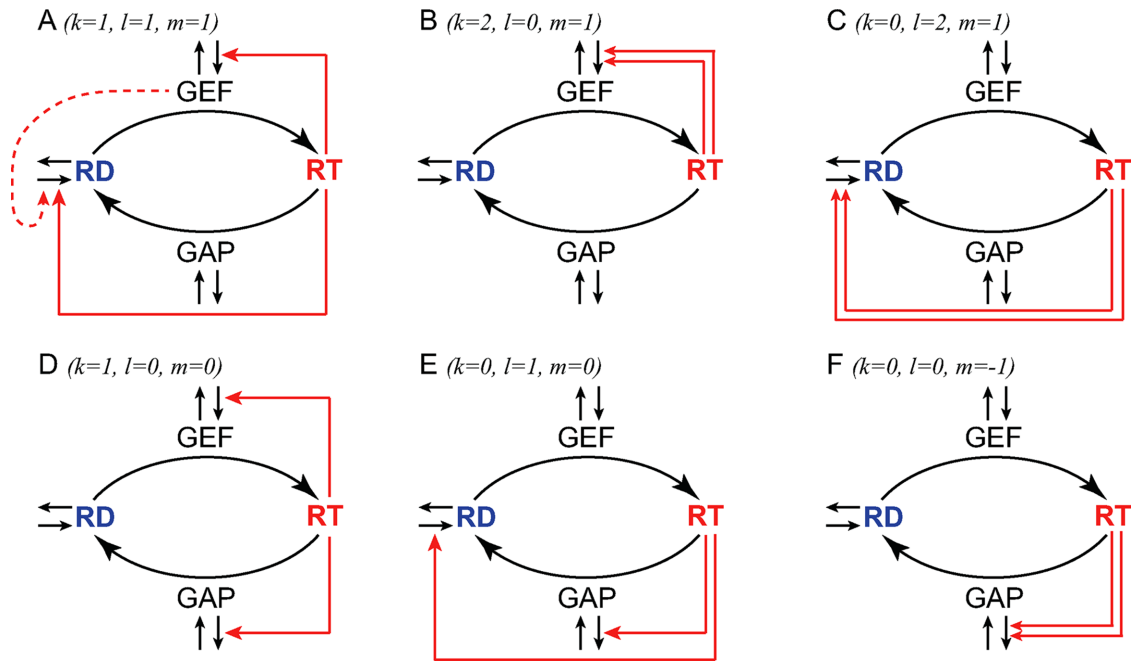
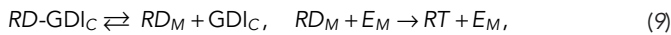


FIGURE 3: Six classes of Cdc42 polarization models with spontaneous symmetry breaking. Feedback loops connecting the active form of Cdc42 (RT) to its regulators and the recruitment of inactive Cdc42 (RD) are shown by red arrows. Double red arrows indicate nonlinear positive feedback. See text for detailed discussion.



It is easy to show that the net effect of reactions 6 and 8 is the same as that of reactions 6 and 7. Notice, however, that if cytoplasmic Cdc42-GDP is bound to a GDI, reaction 8 implicitly assumes formation of a heterotrimeric complex GEF-RD-GDI, which is believed to be prohibited by a significant overlap of the binding sites for GEF and GDI on the GTPase (Hoffman *et al.*, 2000; Rossman *et al.*, 2005). If GDI is taken into the consideration explicitly and reaction 8 is split into two consecutive steps that no longer require the existence of the heterotrimeric GEF-RD-GDI complex (Robbe *et al.*, 2003),



the Wedlich-Söldner-Frey model can no longer explain symmetry breaking. This caveat does not apply, however, to class A models that do not require direct recruitment of RD by a GEF. The model by Ozbudak *et al.* (2005) without additional actin-mediated negative feedback can be also assigned to class A even though the authors did not suggest any explicit molecular mechanism.

Model B. Nonlinear feedback via recruitment of GEF ($k = 2, l = 0, m = 1$)

Another way to achieve dependence of the Cdc42 activation rate on RT^2 is to propose that the feedback loop that recruits GEF is nonlinear (Figure 3B; Liu and Barabasi, 2016). For example, this would be the case if the effector or the effector complex (Figure 2B) that recruits a GEF can simultaneously bind to two molecules of Cdc42-GTP (Khan and Menetrey, 2013; Rai *et al.*, 2016). Of interest, Scd2 has been reported to bind two Cdc42-GTP molecules via its two adjacent SH3 domains (Endo *et al.*, 2003; Wheatley and Rittinger, 2005), but this 1:2 binding stoichiometry has not been seen for Bem1. The Bem1-Cla4 effector complex (Kozubowski *et al.*, 2008), in principle, could bind two active molecules of Cdc42 via

effector domains of Bem1 and Cla4 (Bose *et al.*, 2001; Takaku *et al.*, 2010). However, this hypothetical bivalent interaction appears to be nonessential because *BEM1* deletion mutant was rescued by a GEF-effector chimera containing only a single effector domain of Bem1 (Kozubowski *et al.*, 2008).

Goryachev and Pokhilko (2008) provided the first detailed mathematical analysis of the biochemical mechanism of symmetry-breaking Cdc42 polarization. They assumed that diffusive transport of Cdc42-GDP in complex with GDI follows mechanism 9. In this scenario, delivery of Cdc42-GDP to the site of polarization is governed by the competition between GEF and GDI for inactive GTPase (Robbe *et al.*, 2003; Schoebel *et al.*, 2009; Wu *et al.*, 2010b; Freisinger *et al.*, 2013) but does not involve direct recruitment of RD via either RT (reaction 7) or GEF (reaction 8). Further, they suggested that interaction 6 between the cytosolic Bem1 (or Bem1-Cdc24 complex) and membrane-bound Cdc42-GTP should also occur on the membrane (Goryachev and Pokhilko, 2006), that is,



From relation 6, it follows that the concentration of membrane-bound GEF is proportional to the local concentration of Cdc42-GTP ($E_M \sim RT$). The mass-action rate law applied to reaction 10 then gives us that the concentration of the RT- E_M complex at the polarization site is proportional to $E_M(RT) \cdot RT \sim RT^2$, and thus the feedback via Bem1-Cdc24 recruitment is nonlinear. Only a fraction of the GEF-effector complex is required to be in the complex with Cdc42-GTP at any time for the symmetry breaking to occur in the model. In theory, if Cdc42-GTP formed RT- E_M only with the cytoplasmic Bem1-Cdc24 and, for some unknown reason, could not interact with the membrane-bound GEF, the model would lose its symmetry-breaking property. In practice, this is hardly a limitation of the model because it provides robust symmetry breaking even if the on rate of the reaction between E_M and RT is $<1/30,000$ of that for the reaction between E_C and RT.

The Goryachev–Pokhilko model has been tested experimentally and, with minor modifications and additions, has been extensively used in the literature (Howell *et al.*, 2009; Layton *et al.*, 2011; Savage *et al.*, 2012; Jose *et al.*, 2013; Okada *et al.*, 2013; Wu *et al.*, 2013, 2015; Woods *et al.*, 2015, 2016). A very similar model of this class with Bem1-mediated nonlinear feedback $[GEF] \sim RT^2$ has been proposed by Park, Chou, and colleagues (Lo *et al.*, 2013; Lee *et al.*, 2015). Freisinger *et al.* (2013) questioned the existence of the complex RT-E predicted by the Goryachev–Pokhilko model. They reasoned that because Cdc24 is in complex with Cdc42-GTP, the membrane–cytoplasmic shuttling of Cdc24 should depend on Cdc42 activity. Indeed, with the originally published set of model parameters (Goryachev and Pokhilko, 2008), nearly all of the Cdc24 on the membrane was within the RT-E complex. Freisinger *et al.* (2013) measured Cdc24 fluorescence recovery after photobleaching (FRAP) recovery time in $\Delta bem2$ cells, which exhibit heightened Cdc42 activity because they lack Cdc42 GAP Bem2, and found no difference in comparison with control cells. This observation *per se* does not invalidate the model because, with a different set of reaction rate parameters, the model enables symmetry breaking with <10% of Cdc24 within the RT-E complex. Such low relative abundance of the complex would make it hard to detect the dependence of Cdc24 FRAP on Cdc42 activity.

Model C. Nonlinear feedback via recruitment of RD ($k = 0, l = 2, m = 1$)

Could symmetry breaking occur if Cdc42-GTP did not recruit its GEF? Mathematically, this is possible, for example, if the feedback loop that recruits Cdc42-GDP to the site of polarization is nonlinear, that is, if $RD \sim RT^2$ (Figure 3C). Li, Rubinstein, and colleagues proposed a model of this class (Smith *et al.*, 2013). They postulated that the relationship $RD \sim RT^2$ represents the Cdc42-GTP-dependent release of Cdc42-GDP from the complex with Rdi1; however no specific molecular mechanism providing the required quadratic dependence on RT was suggested. Of interest, their model could be potentially explained by the vesicle-based transport of Cdc42. Indeed, two subunits of budding yeast exocyst, Sec3 and Exo70, have been reported as the interactors of Cdc42-GTP and phosphoinositide lipids (Zhang *et al.*, 2008; Wu *et al.*, 2010a). Bivalent binding of the single exocyst complex to two molecules of RT would provide the required quadratic dependence $RD \sim RT^2$ (Figure 2B). Even if only one of the two exocyst subunits interacts with Cdc42-GTP directly but the binding of the other to the membrane requires negatively charged lipids and their enrichment at the polarization site is downstream of Cdc42 activity (Figure 2C), the required quadratic relationship still stands. A model of Cdc42 polarization during mating (Hegemann *et al.*, 2015) can be also allocated to this model class. Although this model did not explicitly consider Cdc42 nucleotide cycling, it proposed that polarization is achieved by a nonlinear feedback via Cdc42 recruitment.

Model D. Converging linear feedback via GEF and GAP ($k = 1, l = 0, m = 0$)

Symmetry breaking can arise not only from feedback regulation of Cdc42 activators but also from that of its inactivators, GAPs. One class of models of this type requires a linear feedback loop (6) that provides recruitment of a GEF and another linear feedback loop that involves negative regulation of the localization or activity of a GAP (Figure 3D). For example, if only the membrane-bound fraction of a GAP can inactivate Cdc42-GTP and local activity of Cdc42 increases the rate of GAP dissociation from the membrane, for example, via phosphorylation of GAP by an effector kinase,



we find that the rate of Cdc42 inactivation can be expressed as

$$F_{\text{inact}} = \frac{k_A \cdot A_C \cdot RT}{K + RT} \quad (12)$$

This relationship means that at the site of polarization, where the concentration of RT is high, the rate of Cdc42 inactivation saturates and, at this location, is no longer dependent on RT ($m = 0$), so only a simple linear feedback via GEF recruitment would suffice to overcome RT inactivation and enable symmetry breaking. Remarkably, expression 12 has a familiar Michaelis–Menten form, which implies that the requirement for negative regulation of a GAP can be replaced by the requirement that the GAP at the site of polarization is saturated by its substrate, RT. Both mechanistic assumptions produce mathematical expressions of exactly the same form as expression 12.

To the best of our knowledge, models of this type have not yet been proposed in the literature, possibly because exclusion of Cdc42 GAPs from the site of polarization has not been seen in budding yeast. On the contrary, several of these GAPs have been reported to localize to the site of Cdc42 polarization at various stages of bud morphogenesis (Caviston *et al.*, 2003; Knaus *et al.*, 2007; Tong *et al.*, 2007). However, in fission yeast, both known Rho GAPs with activity toward Cdc42-GTP, Rga4 and Rga6, localize in a pattern complementary to that of Cdc42-GTP (Das *et al.*, 2007; Tatebe *et al.*, 2008; Revilla-Guarinos *et al.*, 2016). Although the exclusion of Rga4 relies, at least in part, on the activity of the fission yeast polarity landmark pathway (Kokkoris *et al.*, 2014), it remains to be seen whether activity of Cdc42 is directly or indirectly involved in excluding the GAPs from the site of polarization.

E. Converging linear feedback via RD and GAP ($k = 0, l = 1, m = 0$)

This model class attributes symmetry breaking to the convergence of the two already discussed feedback loops: via recruitment of inactive form of Cdc42 and exclusion of inactivating GAP (Figure 3E). Again, the two feedback loops need not be mechanistically independent. For example, polarized insertion of secretory vesicles guided by Cdc42 activity could potentially deliver inactive Cdc42 and, at the same time, dilute the local concentration of membrane-bound GAPs. For the dilution mechanism to be effective, GAPs need to diffuse on the membrane very slowly, for example, due to association with polymeric cytoskeletal structures. The dilution effect due to Cdc42-driven polarized exocytosis is essential for the formation of the nascent septin ring (Okada *et al.*, 2013). Okada *et al.* (2013) identified a pool of GAP Bem2, which was associated with septin polymer and was no longer detectable in the temperature-sensitive septin mutant *cdc12-6* at a nonpermissive temperature. Failure to maintain a sufficiently high rate of exocytosis resulted in the coalescence of the nascent septin ring into a continuous cap and abrogation of Cdc42 activity at the polarity site. Of interest, Revilla-Guarinos *et al.* (2016) reported that reduction of Rga6 density at the tips of growing fission yeast cells depended on the presence of actin cables. Because actin cables dramatically accelerate polarized exocytosis, it is tempting to speculate that Rga6 exclusion is associated with localized insertion of membrane.

F. Nonlinear feedback via GAP exclusion ($k = 0, l = 0, m = -1$)

Is it possible to have cell polarization without local recruitment of both GEF and the GTPase? Although experimental evidence for this type of model is lacking, a theoretical possibility exists if we assume that exclusion of GAPs from the site of polarization depends

on the square of the local concentration of Cdc42-GTP (Figure 3F). Following the same line of reasoning as in Eqs. 11 and 12, we arrive at

$$F_{\text{inact}} = \frac{k_A \cdot A_C \cdot RT}{K_1 + K_2 \cdot RT + RT^2} \quad (13)$$

which states that, due to the nonlinear exclusion of GAPs, the rate of Cdc42 inactivation decreases rather than increases with Cdc42-GTP concentration. This instability ensures spontaneous polarization of Cdc42 activity. As before, the nonlinearity may arise due to, for example, the existence of a molecular complex that incorporates several Cdc42 effectors and provides local exclusion or inhibition of GAPs.

HOW MODELING HELPS IN UNDERSTANDING CELLULAR POLARIZATION

Mathematical modeling has been instrumental in revealing common principles underpinning cellular polarization in various systems (Iglesias and Devreotes, 2008; Jilkin and Edelstein-Keshet, 2011; Mogilner et al., 2012). Many models describing cellular polarization rely on the reaction-diffusion mechanisms and are both dependent on and independent of the activity of small GTPases (Levchenko and Iglesias, 2002; Dawes and Munro, 2011; Griffin et al., 2011; Lin et al., 2012; Semplice et al., 2012). A rapidly growing cohort of studies also has begun to address the mechanochemical mechanisms of cell polarization (Tostevin and Howard, 2008; Goehring et al., 2011; Lomakin et al., 2015; Maiuri et al., 2015).

Studying GTPase-based polarization of motile cells, Edelstein-Keshet and colleagues focused their attention on “wave pinning,” a stimulus-induced symmetry-breaking behavior that they studied in models that can exhibit bistability of the reaction mechanism (Mori et al., 2008, 2011; Holmes and Edelstein-Keshet, 2016). This type of bistability can occur in spatially homogeneous systems and should be distinguished from the type of bistability shown in Figure 1E, where the two states of the system, polarized and unpolarized, can be exhibited only by spatially extended systems with diffusion. Nevertheless, there is no qualitative divide between these models and the models exhibiting spontaneous symmetry breaking (Trong et al., 2014; Holmes and Edelstein-Keshet, 2016; Nirody and Rangamani, 2016). In fact, all wave-pinning models published so far, under variation of parameters, can also exhibit absolute loss of stability, or Turing instability. Conversely, all models that originally focused on Turing-type behavior can also exhibit wave pinning. In general, if a model can support symmetry breaking (Figure 1E), stimulus-induced and spontaneous symmetry breaking are found within adjacent domains of parameters, so that the wave-pinning structure transforms smoothly into the Turing structure as the parameters vary. Similarly, bistability of the reaction mechanism is neither necessary nor sufficient for polarization. Instead, reaction bistability and formation of a spatial structure are two types of symmetry-breaking behavior that commonly arise in nonlinear systems with positive feedback. Therefore they often co-occur in the same polarity models within overlapping but not coinciding parameter domains.

What have we learned from the mechanistic models of Cdc42 polarization? Here we demonstrated that layout of the biochemical network that controls the dynamics of Cdc42 readily supports symmetry-breaking behavior, such as bistability and polarization. This behavior occurs when the regulators of GTPase activity are wired into converging positive feedback loops. Native or synthetic GTPase effectors can provide this wiring by connecting active form of the GTPase to its regulators. A minimum network layout that permits

symmetry breaking consists of either two converging linear feedback loops or a single nonlinear feedback (Figure 3). All combinations of such feedback loops based on the recruitment of the GTPase itself and its GEF and exclusion of GAPs generate six distinct model classes. Within each class, multiple model flavors can be proposed on the basis of specific assumptions on the molecular mechanisms that implement the feedback loops.

It is not uncommon that theory offers more possibilities than are actually implemented in the real world. Which of the considered model classes are better supported by the existing experimental evidence? A positive feedback loop based on the recruitment of a GEF is possibly the best-studied element of the symmetry-breaking mechanism (Gulli et al., 2000; Bose et al., 2001; Butty et al., 2002; Irazoqui et al., 2003; Kozubowski et al., 2008). Scaffold-effector Bem1 (Scd2 in fission yeast) was found to be a critical element of this feedback as the molecular link between the GEF and the GTPase. Deletion of *BEM1* causes a pronounced phenotype but is not lethal as far as cells express Ras-like GTPase Rsr1/Bud1 (Irazoqui et al., 2003). Despite an impressive body of evidence that supports Bem1-mediated feedback, its existence was challenged, chiefly on the basis of claim that, contrary to the previous data, double-knockout $\Delta\text{rsr1}\Delta\text{bem1}$ is viable (Smith et al., 2013). The following study that used the same strain, however, did not confirm this claim (Woods et al., 2015). Another strong argument in support of the crucial role of Bem1 in symmetry breaking was provided in a recent study that used an optogenetic technique to rapidly and reversibly recruit Bem1 to mitochondria (Jost and Weiner, 2015). This study demonstrated that 80% of cells that were unpolarized before Bem1 sequestration completely failed to polarize in the presence of light, even with intact *RSR1*. Regardless of the specific molecular roles of Bem1 and Scd2, recruitment of GEFs Cdc24 and Scd1 into the respective polarity clusters is firmly established. Taken together, these facts strongly argue in favor of models A, B, and D, which rely on feedback via GEF recruitment (Figure 3).

Is the Bem1 (Scd2)-dependent pathway the only mechanism that provides recruitment of GEF Cdc24 (Scd1)? Fission yeast cells deleted for *scd2* no longer localize Scd1 to the tips but continue to exhibit tip-localized Cdc42-GTP clusters, albeit with reduced activity (Kelly and Nurse, 2011). In budding yeast, it has been long known that *BEM1* genetically interacts with *RSR1* (Chant and Herskowitz, 1991). Furthermore, the $\Delta\text{rsr1}\Delta\text{bem1}$ mutant is synthetic lethal (Irazoqui et al., 2003). If Rsr1 was merely transmitting the spatial information encoded by the nonessential budding landmarks, genetic interaction of *BEM1* and *RSR1* would be difficult to interpret (Wu et al., 2013). Of interest, two studies found that Bud5, an Rsr1 GEF, rapidly relocates during Cdc42 polarization from the landmark-determined ring that surrounds the bud scar into the Cdc42-GTP cluster itself (Kang et al., 2001; Marston et al., 2001). This result suggests a molecular mechanism that recruits Bud5 to Cdc42-GTP. Together with the well-characterized interaction between Cdc24 and Rsr1-GTP (Park et al., 1997; Shimada et al., 2004), this hypothetical mechanism would form a positive feedback loop in which Cdc42 and Rsr1 mutually activate each other by recruiting their respective GEFs. If proven correct, this attractive hypothesis would mean the existence of two parallel feedback loops that recruit Cdc24 to Cdc42-GTP.

Is the GEF-mediated positive feedback loop sufficient to enable symmetry breaking? Indeed, model B suggests this by pointing out that the biochemical mechanism of this feedback is nonlinear. Although model B is consistent with the experimental data, it may not be all-inclusive. Because multiple mechanisms have been proposed to increase membrane deposition of Cdc42 downstream of

Cdc42 activity via both diffusive and vesicle-mediated transport, it is highly likely that model A is also involved in yeast cellular polarization. In fact, the two model classes need not be mutually exclusive but instead could operate in parallel. Indeed, models A and B share the same feedback loop via recruitment of a GEF. In addition, model A incorporates parallel feedback loops based on Cdc42 transport, which may increase the robustness of polarization. Model D, introduced here, also deserves attention. Although it may not be relevant to Cdc42 polarization in budding yeast, it may operate, for example, in fission yeast, either on its own or in parallel with model A. The latter, judging by its robust generic layout, could be a recipe for Cdc42 polarization across multiple species, beyond yeasts. A recent report of tight spatiotemporal correlation between Cdc42 activation and its release from the complex with a GDI in motile mammalian cells suggests a possibility of feedback loops based on GTPase diffusive transport also in higher eukaryotes (Hodgson *et al.*, 2016).

CONCLUSION

Summing up the discussion, we conclude that the existing experimental data do not unequivocally select a single model class. Instead, in its present state, our knowledge suggests the possibility that several parallel and mutually nonexclusive polarization mechanisms are encoded by the genomes of eukaryotes, even as “simple” as yeasts. These mechanisms are likely not deployed equally within and between different species, with one of them gaining dominance while others are “down-regulated” in the course of evolution. Genetic deletions can result in compensatory changes in the expression of other pathway components (Cerikan *et al.*, 2016). This could explain, for example, why acute optogenetic sequestration of Bem1 produces a much stronger phenotype than its genetic deletion (Jost and Weiner, 2015). Compared to traditional knockouts, synthetic proteins bring both a higher level of system control and as-yet-underappreciated potential increase in the system’s complexity. By disrupting one polarization mechanism, a synthetic molecule could potentially enable a bypass mechanism that was either disabled or nonexistent in the native organism. These potential synthetic effects should be carefully considered when planning and interpreting the results of cell-re-wiring experiments.

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